Dynamic Escape Game

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ABSTRACT

We introduce Dynamic Escape Game (DEG), a tool that provides emergency evacuation plans in situations where some of the escape paths may become unavailable at runtime. We formalize the setting as a reachability two-player turn-based game where the universal player has the power of inhibiting at runtime some moves to the existential player. Thus, the universal player can change the structure of the game arena along a play. DEG uses a graphical interface to depict the game and displays a winning play whenever it exists.

ACM Reference Format:

1 INTRODUCTION

Game theory is a well-developed branch of mathematics, largely applied in computer science to reason about the strategic behavior of reactive systems [1, 13]. These are characterized by an ongoing interaction between two or more entities, modeled as players, and the behavior of the whole system deeply relies on this interaction [8]. To reason about resource constraints, quantitative games have been considered [4, 5]. Accordingly, games are played on weighted graphs, where edges are equipped with integer values modeling rewards or costs. Well-stated quantitative games are Mean-Payoff [6] and Energy Games [5]. In this paper, we consider a variant of weighted two-player turn-based reachability games. These are games with weighted transitions in which Player₁ (P₁) tries to reach a target state while Player₂ (P₂) tries to prevent it. Along a play, P₁ plays as usual, i.e. from his current position, he chooses one of the available successors and moves to it. Conversely, P₂, sitting on a set of states S, chooses some of its successors that become irrevocably unavailable to P₁ and added to S. The game starts with S being the initial state for P₂ (different from the one for P₁). P₂ chooses successors under the constraint that the sum of the weights along the involved edges is lower to a given bound. Note that P₂ can dynamically change the structure of the game. The introduced game framework takes inspiration from [20] and it can be usefully applied to solve questions in planning, rescue, and traffic control. Other applications and similar reasoning can be found in [2, 3, 9–12, 14–19]. To solve the above game, we introduce the tool Dynamic Escape Game (DEG). The solution of the game is based on the computation of two priority functions, one for each player, representing their best performing strategies respectively. Our empirical evaluation shows that the priority functions computed by DEG use good heuristic and have excellent runtime execution.

2 GAME STRUCTURE

Our tool works over two-player turn-based games, on weighted graphs under the reachability condition (2TGW, for short).

Definition 2.1. A 2TGW is a tuple $G = (P, I₁, I₂, St, E, T, w, b)$, where $P = \{P₁, P₂\}$ is the set of players, $I₁$ is the initial state for $P₁$, $St$ is the set of states, $E \subseteq St \times St$ is the set of edges, $T \subseteq St$ is the set of the target states, $w : E \rightarrow \mathbb{N}$ is a function that gives an edge returns its weight, and $b$ is a bound.

Given a game $G$, the players move in turn, starting from their starting states, with $P₁$ moving first. The game makes use of a set $S$ containing states that are unavailable to $P₁$ along a play. The game starts with $S = \{I₂\}$ and only $P₂$ can operate on it by possibly adding states. If the game is at $P₁$’s round, given the current state $s$, $P₁$ can move in any successor state of $s \in St$, but those in $S$. If the game is at $P₂$’s round then he can add to $S$ any set $S' \in St \setminus S$ of states reachable from $S$ whose sum of the weights of the traversed edges is not greater than $b$. A configuration is a couple $(s, S) \in St \times 2^{St}$ where $s \notin S$. By $C$ we denote the set of all configurations. A play is a finite sequence of configurations $\pi = (s₀, S₀), \ldots, (sₙ, Sₙ)$, such that $s₀ = I₁$, $S₀ = \{I₂\}$, $S₁ \subseteq S₁+1$, $(sᵢ, Sᵢ+1) \in E$, and for all $s' \in Sᵢ+1 \setminus S₁$ there exists $s \in S₁$ such that $(s, s') \in E$, where $0 \leq i < n$. Note that the maximum length of a play is $n = |St| - 1$, since in the worst case $|S₀| = |St| - 1$. A $P₁$ strategy is a function $σ₁ : C \rightarrow St$ such that for all $(s, S) \in C$ it holds that $σ₁(s, S) \notin S$ and $(s, σ₁(s, S)) \in E$. A $P₂$ strategy is a function $σ₂ : C \rightarrow 2^{St}$ such that: i) for all $(s, S) \in C$ and for all $s' \notin σ₂(s, S) \setminus S$ there exists $s \in S$ such that $(s, s') \in E$; ii) it holds that $Σₙ(s, s') ∈ E(w(s, s')) < b$, where $w \in S$ and $s' \in σ₂(s, S)$. Given $P₁$ strategy $σ₁$ and $P₂$ strategies $σ₂$ they induce a play $π = (s₀, S₀), \ldots, (sₙ, Sₙ)$ such that for all $0 \leq i \leq n$, $sᵢ₊₁ = σ₁((sᵢ, Sᵢ))$ and $Sᵢ₊₁ = σ₂(sᵢ, Sᵢ))$. Finally, $P₁$ (resp., $P₂$) wins the game $G$ if there exists a $P₁$ (resp., $P₂$) strategy such that for all $P₂$ (resp., $P₁$) strategies, the induced play $π = (s₀, S₀), \ldots, (sₙ, Sₙ)$ allows $P₁$ (resp., prevents $P₁$) to visit a target state.

3 HOW TO COMPUTE THE STRATEGIES

In this section we describe the two functions we implemented in our tool which are used by the players to select the strategies to win the game. Let $dist(x, y)$ be the smallest distance w.r.t. the number of edges from $x$ to $y$, $v$ the current state of $P₁$, and $S$ the set of

states of $P_2$. The priority function $\delta_1$ for $P_1$ works as follows: (1) The distances between $S$ and target states are calculated. For each $t \in T$, such a distance is set as $\min_{s \in S} \{\text{dist}(s, t)\}$ and calculated by applying a BFS algorithm on the transpose graph for each $t \in T$ and by choosing the smallest value, which we call $\text{distP}(t)$. (2) The distances between each state $s$ such that $(v, u) \in E$ and each state $t \in T$ are calculated by using the BFS algorithm. So, if the state $u$ cannot reach any target state, $u \in E \setminus t \setminus \{\}$. Finally, $u$ is colored with red. Instead, if a target state $t \in T$ exists such that $\text{dist}(u, t) \leq \text{distP}(t)$, then $u$ is colored with green since $P_2$ cannot block $P_1$ to reach $t$. Finally, $u$ is colored with yellow if $\text{dist}(u, t) > \text{distP}(t)$. Using the priority function $\delta_1$, $P_1$ chooses a green state, if such a state exists, otherwise he chooses a yellow state with the smallest distance between $u$ and a state $t \in T$. The priority function for $P_2$ works as follows: (1) The distances between $v$ and each state $t \in T$ are calculated by applying the BFS algorithm. (2) For each $v \in S$ and for all $u$ such that $(s, u) \in E$, the distance between $u$ and the target states is calculated by using the BFS algorithm. Moreover, a priority, i.e. an integer value between 0 and 3, is associated to $u$ in this way: (i) if $u \in T$ and $(v, u) \in E$, then the priority of $u$ is 3. Instead, if $(v, u) \not\in E$ the priority of $u$ is 1 because $P_2$ is in advantage on this state; (ii) if there is a $t \in T$ such that $\text{dist}(u, t) < \text{dist}(v, t)$ and the constraint on the edges holds then the priority of $u$ is 2. (iii) if there is no $t \in T$ such that $\text{dist}(u, t) < \text{dist}(v, t)$, then the priority of $u$ is 0 because $P_1$ could escape anyway in $t$. Using the priority function described above, $P_2$ chooses a state starting from those with higher priority up to a smallest priority, as long as the sum of the weights of the edges is not over the bound.

**Complexity result.** Given a configuration $(s, S) \in C$, the above algorithm computes the priority functions $\delta_1$ and $\delta_2$ in $O(|V|^2 \cdot (|V| + |E|))$. Since in the worst case the number of rounds of the game is $|V|$, the overall complexity is $O(|V| \cdot |V|^2 \cdot (|V| + |E|))$.

# 4 THE TOOL

The GUI is depicted in Fig. 1. It consists of two parts: the Output Area (OA) and the Control Panel (CP). The OA is made of two frames. The one on the left side is used to depict the game graph. In particular, according to the positions of $P_1$, $P_2$, as well as the target states, the states of the graph are colored in the follow way: purple for $P_1$, red for $P_2$ and blue for the target states. The frame on the right upper side shows all possible paths that $P_1$ can follow starting from its adjacent states and ending to a target state. The CP at the right button corner is composed by five buttons: Manual (M), Random (RD), Clear (C), Restart (RS) and Next (N). The M button is used to build a graph manually. By pressing it, a window pops up in which the user sets the number of states of the game graph. Finally, another window comes out in which the user decides how to connect the states. Finally, the user sets the initial states for $P_1$ and $P_2$ and the target states. The RD button works similarly to the M one, but generates a random game of $n$ states, with $n$ provided by the user. The C button allows to clean the graph area. The RS button allows to restart the current game. Finally, the N button runs automatically a move for the player’s round. Note that there are two ways to move for $P_1$; by pressing the N button or manually.¹

¹A video demonstration is available from https://goo.gl/71FqHF

# 5 BENCHMARKS

In this section we report experimental results to evaluate the performance between DEG and a brute force algorithm, named BF, that uses all possible strategies for $P_1$ and the priority function for $P_2$. Note that we used in BF the priority function for $P_2$ because it is optimal. In particular, we tested the tool on several instances by comparing the priority function with all possible strategies for $P_2$ and we observed that the output in both cases is the same for all instances. The tool² has been implemented in C++ and all tests have been run on an Intel Core i7-6500u with 8 GB of RAM running Microsoft Windows 10. The benchmarks show that over 500 instances, with $17 \leq |S| \leq 21$, DEG returns the correct solution, that is $P_1$ wins in both DEG and BF, in about 91% of the instances. Moreover, as reported in Fig. 2, DEG outperforms the BF algorithm in all the instances. In conclusion, the results show that DEG uses a good heuristic for $P_1$ and an excellent runtime execution.

![Figure 1: The main window of our tool.](image)

**Figure 2: Comparison between DEG and BF w.r.t. running time execution.**

# 6 CONCLUSION

This paper introduces Dynamic Escape Game, a tool solving a specific weighted game under reachability condition, where the opponent can dynamically modify the game arena. To solve the game we have introduced two priority functions to be used by the players. Our benchmarks have showed that our tool exhibits an excellent running-time execution. Also that the introduced priority functions are good heuristics. We believe that our tool can be used as a core engine to practically address real escape problems in MAS.

²The tool is available for download from https://bitbucket.org/antonylogic/deg/
REFERENCES


