

# Attention Actor-Critic algorithm for Multi-Agent Constrained Co-operative Reinforcement Learning\*

Extended Abstract

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## ABSTRACT

In this work, we consider the problem of computing optimal actions for Reinforcement Learning (RL) agents in a co-operative setting, where the objective is to optimize a common goal. However, in many real-life applications, the agents are also required to satisfy certain constraints specified on their actions. Under this setting, the objective of the agents is to not only learn the actions that optimize the common objective but also meet the specified constraints. In recent times, the Actor-Critic algorithm with an attention mechanism has been successfully applied to obtain optimal actions for RL agents in multi-agent environments. In this work, we extend this algorithm to the constrained multi-agent RL setting.

## KEYWORDS

Multi-agent Reinforcement Learning; Attention Mechanism

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## 1 INTRODUCTION

In a multi-agent constrained co-operative RL setting, the agents have to learn actions that not only minimize the expected total discounted cost but also respect the constraints specified. One approach to satisfy the constraints is to construct a modified cost as a linear combination of the original cost and the constraint costs. However, the weights to be associated with the costs are not known upfront and need to be learned in a trial-and-error fashion. We alleviate this problem by considering the Lagrangian formulation of the problem and training dual Lagrange parameters that act as weights for the constraint costs. In this work, we propose an Actor-Critic algorithm for computing the optimal actions for agents that makes use of the attention mechanism. A brief overview of the comparison of our work with other works in the literature is provided in Table 1.

\*Equal contribution by the first three authors. Full paper is available at [20].

References	Features
[7, 11, 16, 18, 19]	Deep RL algorithms for multi-agent setting. Attention mechanism not considered.
[13, 14, 17]	Deep RL algorithms with Attention for multi-agent setting. Constrained setting not considered.
[3–5]	RL algorithms for single-agent constrained setting. Multi-agent constrained setting not considered.
[1, 15, 23]	Deep RL algorithms for single-agent constrained setting. Multi-agent constrained setting not considered.
[2, 6, 9, 10, 12, 21, 22, 24]	RL algorithms for multi-agent constrained setting. Attention mechanism not considered.
<b>Our Work</b>	Deep RL algorithm with Attention mechanism for multi-agent Constrained setting.

**Table 1: Comparison with other works in the Literature**

## 2 MODEL

We now briefly discuss the constrained co-operative multi-agent setting [8] described by the tuple  $\langle n, S, A, T, k, c_1, \dots, c_m, \gamma \rangle$ . Here,  $n$  denotes the number of agents in the environment,  $S = S_1 \times S_2 \times \dots \times S_n$  is the joint state space,  $A = A_1 \times \dots \times A_n$  denotes the joint action space and  $T$  is the probability transition matrix. Single-stage cost function ( $k$ ) where  $k(s, a)$  denotes the cost incurred when joint action  $a$  is taken in state  $s$ . Moreover,  $c_1, \dots, c_m$  denote the single-stage cost functions for the constraints. Note that both the main cost function ( $k$ ) and constraint costs ( $c_1, \dots, c_m$ ) depend on the joint action of the agents. Finally,  $\gamma$  denotes the discount factor. Let  $\pi_i : S_i \rightarrow \Delta(A_i)$  denote the policy of agent  $i$ , where for a given state of agent  $i$ ,  $\pi_i(s_i)$  is a probability distribution over its actions. We now define the total discounted cost ( $J$ ) for a joint policy  $\pi = (\pi_1, \dots, \pi_n)$  as follows:

$$J(\pi) = E \left[ \sum_{t=0}^{\tau} \gamma^t k(s_t, \pi(s_t)) \right], \quad (1)$$

where  $E[\cdot]$  is the expectation over the entire trajectory of states with initial state  $s_0 \sim d_0$ , where  $d_0$  is a given probability distribution

over states,  $\tau$  is a finite stopping time and  $s_t$  is the joint state at time  $t$ . The  $m$  constraints on the system are defined as follows:

$$E\left[\sum_{t=0}^{\tau} \gamma^t c_j(s_t, \pi(s_t))\right] \leq \alpha_j, \forall j \in 1, \dots, m, \quad (2)$$

where  $\alpha_1, \dots, \alpha_m$  are pre-specified thresholds.

The objective of the agents in the multi-agent constrained cooperative RL setting is to compute a joint policy  $\pi^* = (\pi_1^*, \dots, \pi_n^*)$  that is the solution to the optimization problem

$$\begin{aligned} \min_{\pi \in \Pi} J(\pi) &= E\left[\sum_{t=0}^{\tau} \gamma^t k(s_t, \pi(s_t))\right] \\ \text{s.t. } E\left[\sum_{t=0}^{\tau} \gamma^t c_j(s_t, \pi(s_t))\right] &\leq \alpha_j, \forall j \in 1, \dots, m, \end{aligned} \quad (3)$$

where  $\Pi$  is the set of all joint policies. We make use of Lagrangian approach to solve this constrained problem. The pseudo-code of our proposed algorithm is described in Algorithm 1.

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**Algorithm 1** Multi-Agent Constrained Attention Actor-Critic (MACAAC)

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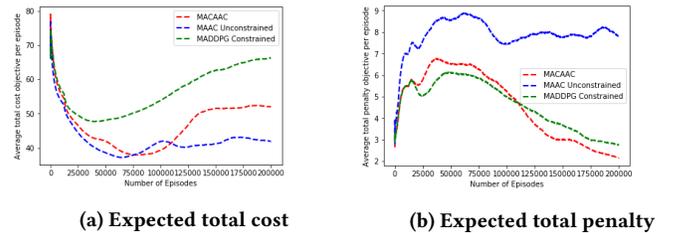
- 1:  $E \leftarrow$  Maximum number of episodes.
  - 2:  $L \leftarrow$  Length of an episode.
  - 3:  $U \leftarrow$  Steps per update.
  - 4:  $\theta_i \leftarrow$  policy parameters of the agent  $i$ ,  $i = 1, \dots, n$ .
  - 5: **UpdateCritic**: Subroutine to update the critic parameters.
  - 6: **UpdateActors**: Subroutine to update the policy parameters of all the agents.
  - 7:  $Q_{\eta_j} \leftarrow$  Q-value of constrained cost associated with constraint  $j$ ,  $j = 1, \dots, m$ .
  - 8:  $\beta_t \leftarrow$  Slower timescale step-size at time step  $t$ .
  - 9: Initialize Lagrange parameters  $\lambda_1, \dots, \lambda_m$ .
  - 10: Create  $\mu$  parallel environments.
  - 11: Initialize replay buffer,  $D$ .
  - 12:  $u \leftarrow 0$
  - 13: **for**  $ep = 1, 2, \dots, E$  **do**
  - 14:   Obtain initial observations  $o_i^e$  for all agents  $i$  in each environment  $e$
  - 15:   **for**  $t = 1, \dots, L$  **do**
  - 16:     Obtain actions  $a_i^e \sim \pi_{\theta_i}(\cdot | o_i^e)$ ,  $\forall i = 1, \dots, n$ ,
  - 17:      $\forall e = 1, \dots, \mu$
  - 18:     Execute actions and get  $(o_i^{*,e}, k^e, c_1^e, c_2^e, \dots, c_m^e) \quad \forall i, e$
  - 19:     Let  $r^e = k^e + \sum_{j=1}^m \lambda_j c_j^e, \quad \forall e$
  - 20:     Store  $(o_i^e, a_i^e, r^e, c_1^e, c_2^e, \dots, c_m^e, o_i^{*,e}), \forall i, e$  in  $D$
  - 21:      $o_i^e = o_i^{*,e}, \forall i, e$
  - 22:      $u+ = \mu$
  - 23:     **if**  $(u \% U) < \mu$  **then**
  - 24:       Sample minibatch  $(B)$  from  $D$
  - 25:       Get next actions  $a'_1, \dots, a'_n$
  - 26:       **UpdateCritic** $(B, a'_1, \dots, a'_n)$
  - 27:       **UpdateActors** $(B)$
  - 28:       **for**  $j = 1, \dots, m$  **do**
  - 29:          $\lambda_j \leftarrow \max(0, \lambda_j + \beta_t(Q_{\eta_j} - \alpha_j))$
  - 30:       **end for**
  - 31:     **end for**
  - 32:   **end for**
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### 3 EXPERIMENTS AND RESULTS

In the constrained version of Cooperative Navigation [16] that we consider, there are 5 agents and 5 targets that are randomly generated in a continuous environment at the beginning of each episode. The objective of the agents is to navigate towards the targets in a co-operative manner such that all targets are covered. The length of each episode is 25 time steps and the single-stage cost at each time step is the sum of the distance to the nearest agent, over all the targets. Therefore, the agents have to learn to navigate towards the targets in such a way that all target positions are covered. However, we include a single-stage penalty of 1 when there is a collision between the agents (and 0 otherwise). The penalty threshold ( $\alpha$ ) is set to 3 in our experiments. This means that the expected total penalty over all the episodes must be less than or equal to 3. The discount factor is set to 0.99. We refer to the main cost that the agents are minimizing as ‘cost’ and the constrained cost as the ‘penalty’. For comparison purposes, we also implement the constrained version of MADDPG [16] algorithm, which we refer to as ‘MADDPG-C’. Moreover, to better analyze the results, we also report the results on an un-constrained version of Multi-agent Attention Actor-Critic [13] where there is no penalty incurred for collisions among the agents, which we simply refer to as ‘Unconstrained’.

#### 3.1 Discussion

In Figure 1a, we observe that the total cost approaches convergence for all the three algorithms. The ‘Unconstrained’ algorithm achieves the smallest average cost as there is no penalty for collisions in this case. Therefore, the agents can move freely in the continuous space and navigate quickly towards the targets. This can also be observed in Figure 1b, where we see that the average penalty of the ‘Unconstrained’ algorithm is the highest. In Figure 1b, we see that the average penalty comes down as the training progresses for the constrained algorithms (MADDPG-C and our proposed MACAAC), while for the ‘unconstrained’ algorithm it almost remains constant. This is the effect of Lagrange parameters that are learnt in the constrained setting.



**Figure 1: Performance of Algorithms on Constrained Cooperative Navigation during the training.**

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